

# GPS

Prof. Bharat Lohani

Aman

## GPS Survey

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- ① Reference ellipsoids and Coordinate Systems, GPS Principle, GPS Elements, applications of GPS, advantages and limitations.
- ② GPS Errors, Differential GPS, and advantages.
- ③ GPS: Improving Accuracy, Various modes of Operation.

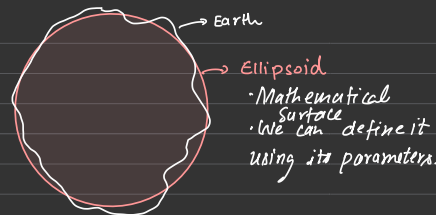
### GPS: Global Positioning System

- GPS provides axis location.  
Where am I? Location  
Where is a particular object?
- GPS can help us to locate our position.
- Position is with reference to something so we need to define a coordinate system.
- GPS makes use of satellites. Using those satellites which are at a certain altitude we can know our position.

[Coordinate System]

### Reference Ellipsoid

- Mathematical surface
- Best fitting to earth
- Same mass and C.G. as of earth
- WGS-84 is one similar ellipsoid



• We fit an ellipsoid to earth because earth is slightly oblate. Oblate means it is not spherical, from the poles it is slightly pressed. On an undulating earth we are fitting an ellipsoid.

• GPS make use of this WGS-84 ellipsoid for measuring the coordinates.

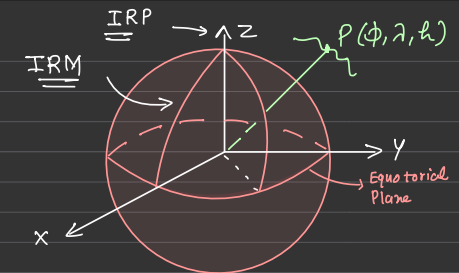
### Geodetic Coordinate System (GCS)

$(\phi, \lambda, h)$

Latitude Longitude Normal height

WGS-84

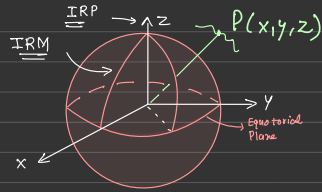
- IRP → IERS Reference Pole  
{International Earth Rotation Service}
- IRM → IERS Reference Meridian
- Right-handed Coordinate System



x → fixed → IRM  
z → fixed → IRP  
y → defined automatically because it is a right handed coordinate system.

## Cartesian Coordinate System

$$(x, y, z)$$

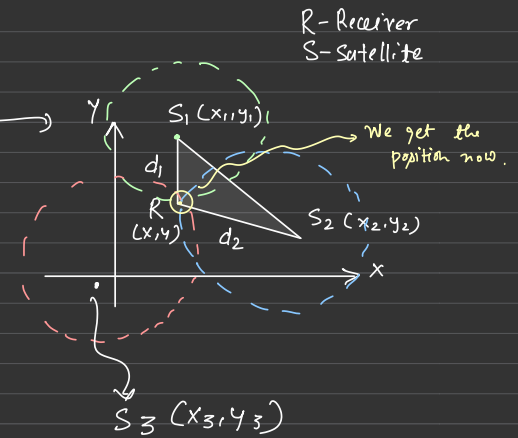


- $(\phi, \lambda, h) \Leftrightarrow (x, y, z)$   
we can determine one from the other.
- GPS will give us measurement in the WGS-84 coordinate system with reference to this geocentric coordinate system either as  $(x, y, z)$  or  $(\phi, \lambda, h)$
- We can transform one from the other.
- In order to understand GPS, we should keep in our mind that yes there is a coordinate system sitting at the centre of earth. (mass centre of earth)

## Principle of GPS

2D Example

- GPS is 3-D
- 3 Satellites
- Distance R-S = ?
- Know where satellites are?



## Distance of GPS Receiver from the Satellite:

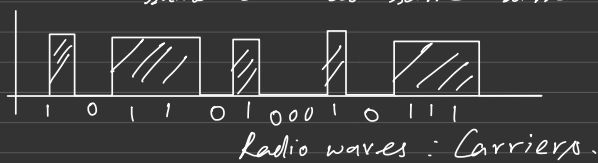
$$d = c \times t \quad \text{Satellites sending radio signals}$$

How is 't' measured?  
Accuracy in 't' important.

- $S \rightarrow R$  ✓
- $R \rightarrow S$  ✗



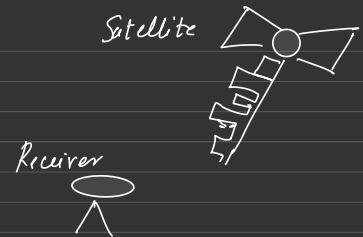
- How do we measure the distance?  
Synchronization of satellite and receiver is used.  
"same code at same time"



PRC  
Pseudo Random Code

$$(1, 2, 3, 4, \dots)$$

$$\underline{t \times c = d}$$

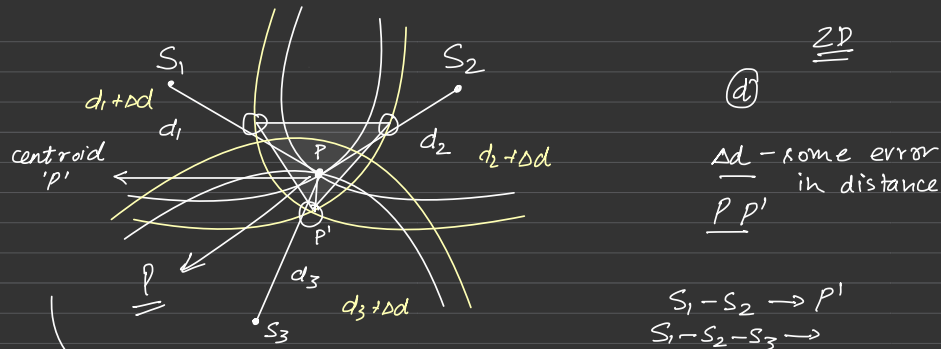


- Time measurement accurately: 4<sup>th</sup> satellite  
Synchronization error in receiver and satellite clock.

Clock Atomic (satellite)

Receiver

Here clock is not atomic one and we want the receiver to be inexpensive so there is not proper synchronization.



3 satellites here can solve the problem for 2-D  
 ⇒ 4 satellite we need to have in 3-D problem.

- Centroid is the point 'P'
- Even if our receiver has synchronization error, still it is possible to determine the coordinate of the point accurately. The error's effect can be eliminated by measuring distances from 4 satellites in GPS.

### Where are the Satellites?

- Satellites are put in stable orbits.
- DoD (Department of Defence) Monitoring
- "Ephemeris" transmitted to satellites.
- Navigation code with signal from satellites.

### GPS Signal

- ⇒ L<sub>1</sub> Carrier - 1227.6 MHz Carrier
- ⇒ L<sub>2</sub> Carrier - 1575.42 MHz

Ranging Code modulated on carriers.

↳ C/A code ⇒ (Clear Access) (Coarse Acquisition) Not Precise  
 at 1.023 MHz → Civil

↳ P Code ⇒ (Private) (Protected) (Precise)  
 at 10.23 MHz → Military

GPS which is mostly used around the world.

### ① NAVSTAR (U.S.A.)

Satellite Constellation: 1994 operational  
 24 satellites: At least 4 above horizon  
 Altitude: 20183 km

### ② Glonass (Russian)

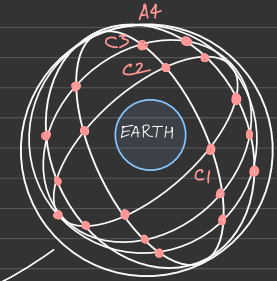
### ③ Galileo (European Union)

visible  
 (we receive signal)

• GPS is a generic term.

• 6 orbits with 4 satellites

A-F → 6 orbits  
 1-4 → 4 satellites

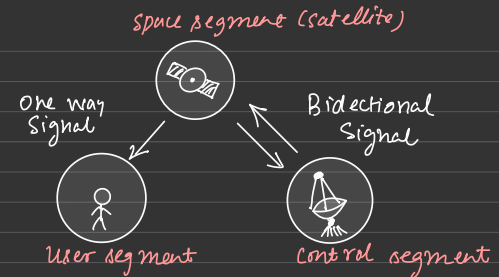


### NAVSTAR

They are positioned in such a way that at any time it, we should be able to see 4 satellites.

### GPS Segments

- Space
- Control
- User



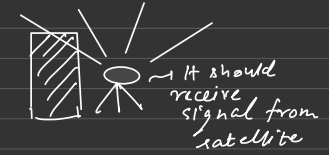
GPS  
 Geodetic  
 GS-5  
 PDA

## Advantages of GPS

- Independent Positioning
  - No intervisibility requirement
  - Independent of Weather Conditions
  - Survey Network (Control Points) as desired.
  - GPS Survey
    - ↳ Flexible
    - ↳ Accurate
    - ↳ Less time consuming
  - Round-the-clock use
  - Global 3D Coordinates
- ↳ We'd fix pts as to make a particular shape becaz of angle. in GPS it isn't so.

## Limitations of GPS

- Expensive
- Cannot be used in:  
Undergrounds, forest, urban area
- Cannot be used in inaccessible areas.

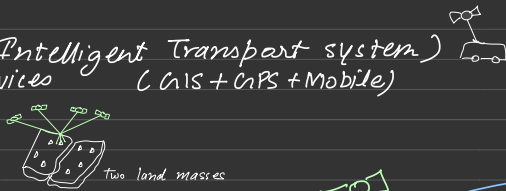


↳ For those areas, we use  
• LiDAR  
• Photogrammetry

## Applications of GPS:

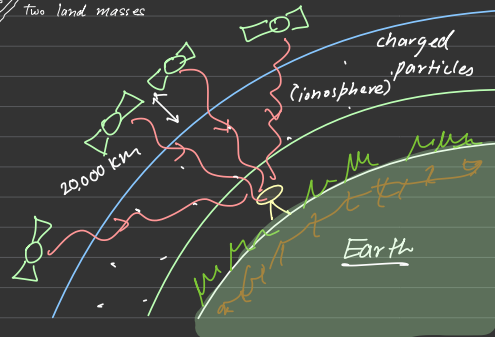
"Wherever location is important"

- Mapping
- Vehicle Navigation (Intelligent Transport system)
- Location Based Services (GIS + GPS + Mobile)
- Earthquake Prediction



## Error in GPS Survey

- ① Satellite Errors
  - Atomic Clock
  - Orbit Error



## ② The atmosphere

- Slowing speed of signal
- Unpredictable variation of atmosphere
- Correction by average atmosphere

Ionospheric-free solution — Dual Frequency L<sub>1</sub>-L<sub>2</sub>

↳ By observing relative slowing of L<sub>1</sub> & L<sub>2</sub>.

## ③ Multipath Error



## ④ Receiver Error

- Clock
- Internal Noise

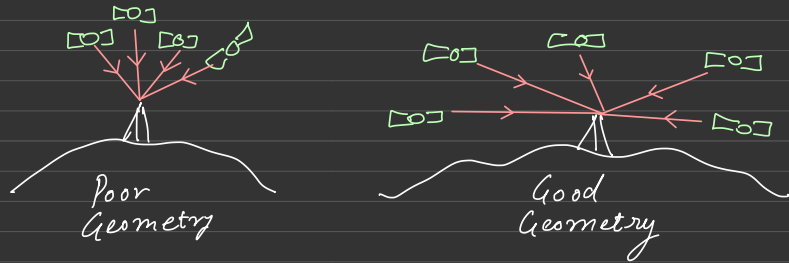
## ⑤ Intentionally Introduced Errors

- Corrupting Satellite Clock with noise
- Corruption in Navigation Data

(Selective Availability) DoD

## ⑥ Geometry of Visible Satellites

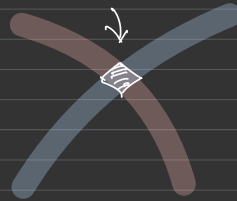
↳ Geometric Dilution of Precision (GDOP)



2D Example



When angle is about 90°, the area of uncertainty is less.



⇒ GDOP is a measure of geometry of satellites  
⇒ A scalar

### Effect of GDOP

User equivalent range error (UERE) -  $\sigma_r$

↳ Measure of accuracy of single pseudo range measurement.

$$\sigma^* = \text{GDOP} \times \sigma_r$$

$\sigma^*$  S.D. of positions

- Smaller GDOP better GDOP < 5 is considered good.

### GPS Services

— SPS (Standard Positioning Service) } Civilian Users  
Based on single  $L_1$  - C/A Code

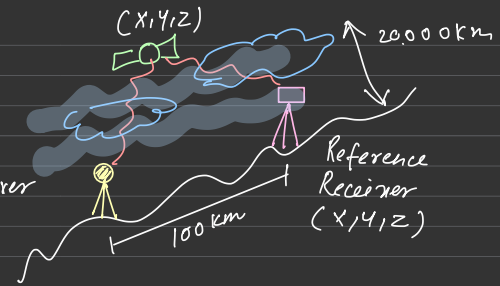
— PPS (Precise Positioning Service) } Military U.S.  
Based on dual frequency - P Code

Accuracy achievable by single G.P.S. (code phase)

	SPS	PPS
Positioning Accuracy	With SA: $\pm 50\text{m}$ Now without SA: $\pm 10\text{m}$	$\pm 5\text{m}$

### Differential GPS (DGPS)

- Error due to ionosphere and troposphere are same. Rover
- both receivers are making use of same satellites → error due to clock is same. Reference Receiver



#### ① Actual Time Computation

$$[(X_1, Y_1, Z_1)_S, (X, Y, Z)_R] = d_{SPR}$$

$$t_a - d_{SPR}$$

Measured time -  $t_m$

$$\text{Error in time } t_a - t_m = \Delta t$$

$\Delta t$  computed for all satellites

- Connections will keep changing.
- Simultaneous observation needed for entire period of survey.

### Processing of data:-

- Post processing of data
- Real time processing of data
  - Error due to latency.

### Beacons as reference receivers?

↳ Transmitting corrections in their local area.

Example:- WAAS (Wide Area Augmentation Service)

- ↳ since 1991
- ↳ on portable GPS 2001

- Some errors can be eliminated by the Differential GPS
- Error because of the receiver or because of the multipath can not be eliminated by differential positioning because that is a local error
- Only errors because of atmosphere or because of the satellite can be eliminated.

### GPS Measurement Techniques

(3)

- ① Code phase based ranging
- ② Carrier phase based ranging → More accurate

### Code based measurement

- Pseudo random code correlation
- Pseudo range determination
- 4 pseudo ranges needed

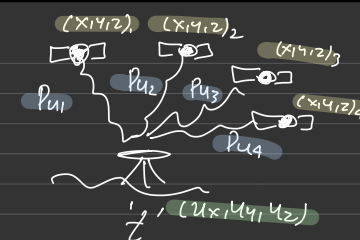
Location of the receiver

c/A code	→ 1.023 MHz	→ 2.93 m	} → ?
P code	→ 10.23 MHz	→ 29.3 m	

Effect



### Computation of Receiver location



$(x_i, y_i, z_i)$  — Location of  $i^{th}$  sat

$Pu^i$  — Pseudo ranges from receiver to satellite  $i$

$dTu$  — Receiver clock error

$$I \quad Pu^1 = \sqrt{(x_1 - x_u)^2 + (y_1 - y_u)^2 + (z_1 - z_u)^2} = cdTu$$

$$II \quad Pu^2 = \sqrt{(x_2 - x_u)^2 + (y_2 - y_u)^2 + (z_2 - z_u)^2} = cdTu$$

$$III \quad Pu^3 = \sqrt{(x_3 - x_u)^2 + (y_3 - y_u)^2 + (z_3 - z_u)^2} = cdTu$$

$$IV \quad Pu^4 = \sqrt{(x_4 - x_u)^2 + (y_4 - y_u)^2 + (z_4 - z_u)^2} = cdTu$$

⇒ Solving provides  $(x_u, y_u, z_u)$  → Location of the receiver

## Carrier phase based measurement

EDMI

$$D = \frac{1}{2} \left( N\lambda + \frac{\Delta\phi}{2\pi} \lambda \right)$$

↳ Active ranging system

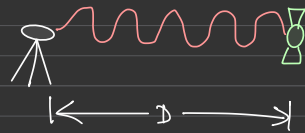
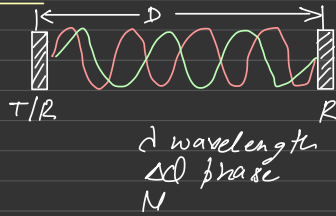
GPS Passive Ranging System

↳

$$D = N\lambda + \frac{\Delta\phi}{2\pi} \lambda$$

$\Delta\phi$  = Difference between received carrier phase and phase of the Quartz Crystal Oscillator in receiver.

Decode Modulation



$$D = N\lambda + \frac{\Delta\phi}{2\pi} \lambda + \text{error}$$

- $\Delta\phi \rightarrow$  measured with high accuracy 3-10 mm

$$\left[ \begin{array}{l} \Rightarrow I_n \\ \Rightarrow \text{Carrier} \end{array} \right. \begin{array}{l} C/A \approx 1 \text{ MHz} \\ \approx 1000 \text{ MHz} \end{array} \left. \begin{array}{l} \text{Implication?} \\ \downarrow \end{array} \right.$$

$$\begin{array}{l} C/A \sim 1 \text{ MHz} \rightarrow 300 \text{ m} \\ \text{Carrier} \sim 1000 \text{ MHz} \rightarrow 0.30 \text{ m} \end{array} \left. \begin{array}{l} \text{by } (c = \lambda f) \\ \downarrow \\ \text{smaller} \\ \downarrow \\ \text{more accurate} \\ \text{position} \end{array} \right\}$$

$$D = N \cdot \lambda + \frac{\Delta\phi}{2\pi} \lambda$$

$$\Delta D \propto \lambda$$

$$\propto \Delta\phi$$

- $N \rightarrow$  How to know  $N$ ? Full cycles

Resolving Carrier phase ambiguity  $\Rightarrow N$   
or Integer ambiguity



Ambiguity resolution  $\Rightarrow$  Value of  $N$ .

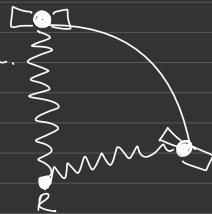
Various algorithms are available

[Locking]

General Steps:

- $\rightarrow$  Need prior value of ambiguity parameters
  - $\hookrightarrow$  Known reference point
  - $\hookrightarrow$  Use of code based pseudo range
- $\rightarrow$  Use of dual frequency and best geometry of satellite.
- $\rightarrow$  After locking  $\Delta\phi$  is measured continuously.
- $\rightarrow$   $N$  remains same for full direction of observation.
- $\rightarrow$  Additional cycles are counted.

Extra Cycles



## Comparison

- Code phase based ranging
  - $\hookrightarrow$  Simple, Fast, No need of initial value
  - $\hookrightarrow$  Less accurate: 300 m
- Carrier phase based ranging
  - $\hookrightarrow$  More accurate
  - $\hookrightarrow$  Complex, Time consuming, Initial value.

## Types of GPS Receivers

- Code phase Receiver
  - Use P or C/A code
  - less accurate
  - Fast
- Carrier phase Receiver
  - $\hookrightarrow$  Use carrier frequency
  - 1. Single frequency
    - $L_1$
    - Cheaper - Ionospheric Error
  - 2. Dual frequency
    - $L_1$  and  $L_2$
    - Eliminates ionospheric Error

CRIS data updation  
1:50,000

$\rightarrow$  Costly

▷ Classification based on data use

- C/A
- C/A + L<sub>1</sub> carrier
- C/A + L<sub>1</sub> carrier + L<sub>2</sub> carrier
- C/A + P + L<sub>1</sub> + L<sub>2</sub>

▷ Classification based on channel

- Multi channel : 8, 12, 24 → can simultaneously lock with many satellites simultaneously.
- Sequential Receiver → one by one
  - ↳ Time consuming
  - ↳ Less accurate
  - ↳ Cheaper

▷ Integrated GPS receiver

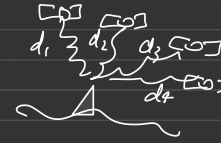
NAVSTAR + GALILEO

GPS Positioning Approaches

1. Point vs. Relative
2. Static vs. Kinematic
3. Real time vs. Post mission

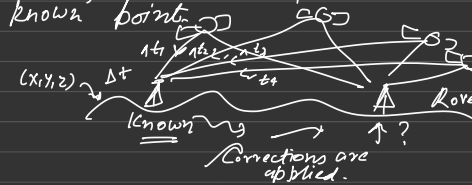
Point Positioning:

- ↳ Single Point Positioning
- ↳ Absolute Positioning



Relative Positioning:

↳ Coordinates of an unknown point with respect to receiver at a known point.



Static: GPS receiver static

Kinematic: GPS receiver moving

Real time positioning: (Real time computation of position)

Single point:

Relative:

- Latency
- Use of broadcast ephemeris.

Post mission positioning:

Single point:

Relative:

(Use of precise ephemeris) → available from website.

Nominal Positioning Accuracies in DGPS

GPS Receiver	Estimated Accuracy	95%	Best accuracy
① Low Cost	Code	3-5 m	n/a
② Geodetic Quality L <sub>1</sub> -L <sub>2</sub> , static	Carrier	0.3-1 m	2 mm ± 1 ppm
③ RTK with Geodetic receiver (Carrier)	Carrier	n/a	10-50 mm

↳ Instrument baseline distance

↳ Post processing